

Pythagorean Triple: $(a, b, c) \in \mathbb{Z}^3$
such that $c^2 = a^2 + b^2$

Theorem: A pythagorean triple exists.

Proof: $c = 5, a = 4, b = 3$. Then $c^2 = a^2 + b^2$.

Fermat Triple: $(a, b, c) \in \mathbb{Z}^3$. $a \neq 0, b \neq 0, c \neq 0$.

so that $c^3 = a^3 + b^3$

Theorem: No Fermat Triple exists.

Proof: Typically by contradiction.

Assume a, b, c satisfies $c^3 = a^3 + b^3$
∴ deduce a contradiction.

$\left[\sim (\exists x, x \text{ Fermat triple}) \right]$

\Leftrightarrow

$\forall x, x$ is not a Fermat triple.